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Information transfer in networks

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Overview

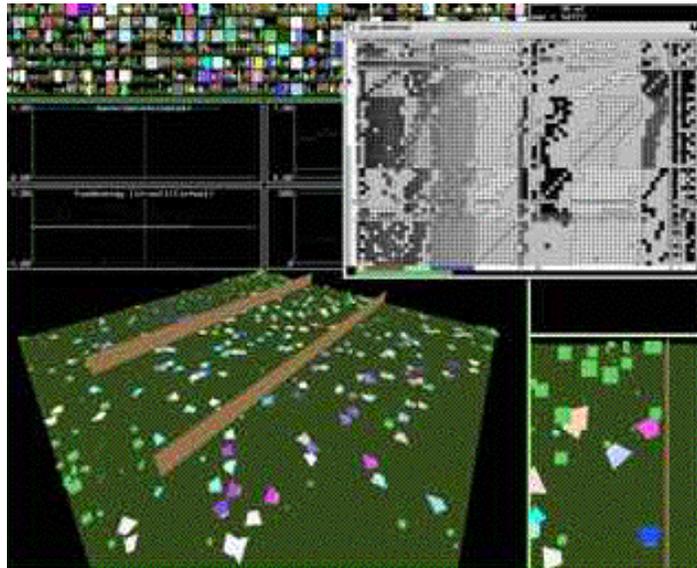
- Two studies regarding information transfer in networks, using this concept for two distinct purposes:
 1. Using known dynamics to infer *logical structure* of nodes in a network
 - Aim: to study what sorts of functional and structural networks evolve in NNs in a computational ecology.
 2. Using known dynamics and structure to analyse *computation* in a network
 - Aim: to characterize the intrinsic computation in cascading failure events in power grids

Contributors

- **Functional and structural topologies in evolved neural networks**
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 - **Information dynamics of cascading failures in power grids**
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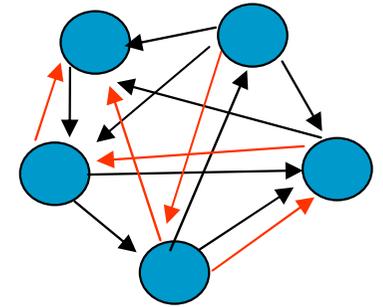
Functional and structural topologies in evolved neural networks

- What sorts of topologies evolve in neural networks in a computational ecology?
 - Studying agents in Polyworld.
 - Examining both known structural networks and inferred functional networks (using MI and TE).
 - Topological analysis of these networks.
 - Results: Trend of more integrated activity across the networks (more “small-world” character with evolutionary time).



Functional networks

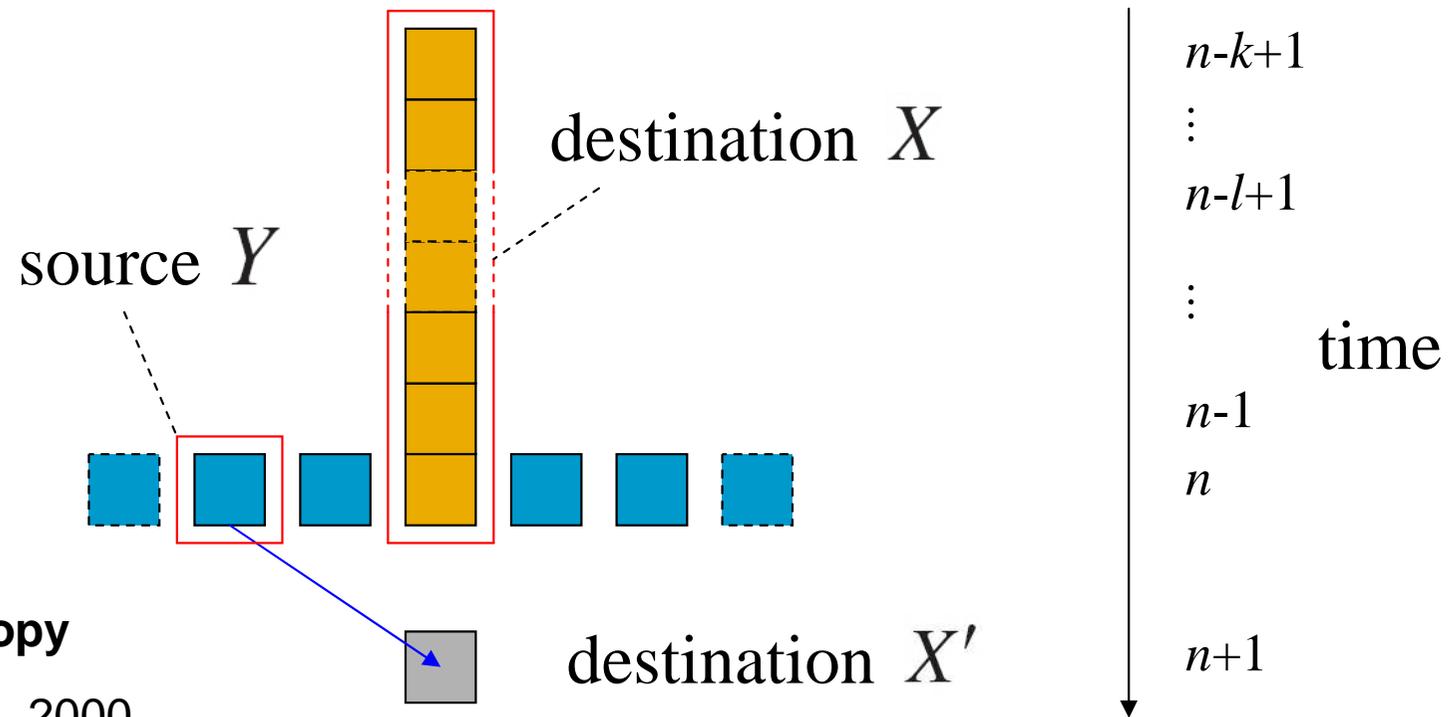
- *Functional connection* := a statistical dependence in time between two nodes
- *Functional network* := a set of functional connections.
- Two step process:
 1. Measuring statistical dependence / closeness
 2. Deciding whether the closeness should constitute a link
- **Why use functional networks:**
 - To infer structural network where it is unknown
 - Insight into the logical structure of the network and how this changes as a function of network activity.
- **Our measures of closeness:**
 - Mutual information $I_{X;Y} = \sum_{x,y} p(x,y) \log_2 \frac{p(x,y)}{p(x)p(y)}$
 - Transfer entropy $T_{Y \rightarrow X} = \sum_{w_n} p(w_n) \log_2 \frac{p(x_{n+1} | x_n^{(k)}, y_n^{(l)})}{p(x_{n+1} | x_n^{(k)})}$



$$w_n = x_{n+1}, x_n^{(k)}, y_n^{(l)}$$

Transfer entropy

$$T_{Y \rightarrow X'} = I(Y; X' | X) = H(X' | X) - H(X' | X, Y)$$



Transfer entropy

Schreiber, PRL 2000.

$$T_{Y \rightarrow X} = \sum_{w_n} p(w_n) \log_2 \frac{p(x_{n+1} | x_n^{(k)}, y_n^{(l)})}{p(x_{n+1} | x_n^{(k)})}$$

$$w_n = x_{n+1}, x_n^{(k)}, y_n^{(l)}$$

Topological measures

- **Assortativity**

- Assortativity is defined as a correlation function in terms of degrees
- Defined in the prev. talk

- **Modularity**

- Network modularity is the extent to which a network can be separated into independent sub-networks
- Quantifies the fraction of links that are within the respective modules compared to all links in a network
- Given an algorithm which can partition a network into k modules, modularity is defined as

$$Q = \sum_{s=1}^k \left[\frac{l_s}{L} - \left(\frac{d_s}{2L} \right)^2 \right],$$

- Here k is the number of modules, L is the number of links in the network, l_s the number of links between nodes in module s , and d_s is the sum of degrees of nodes in module s

- **Closeness centrality**

- Closeness centrality of a node v is defined as the mean geodesic distance (shortest path length) between the node and all other nodes in the network
- We use the non-inverted quantity
- Formally defined as $C^C(v) = \sum d_G(v, t)$

- Where $d_G(v, t)$ is the shortest path distance between nodes v and t .

- **Clustering coefficient**

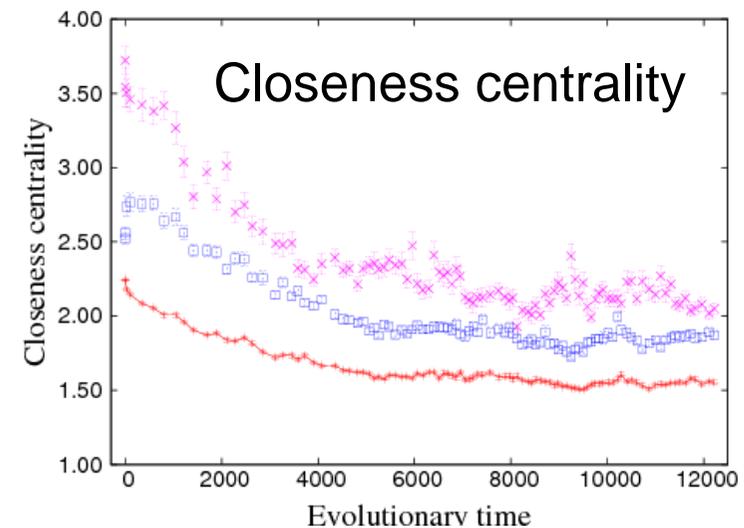
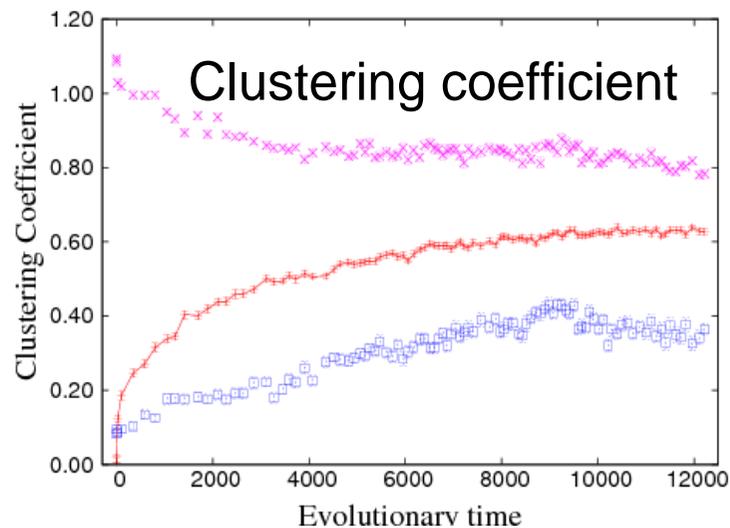
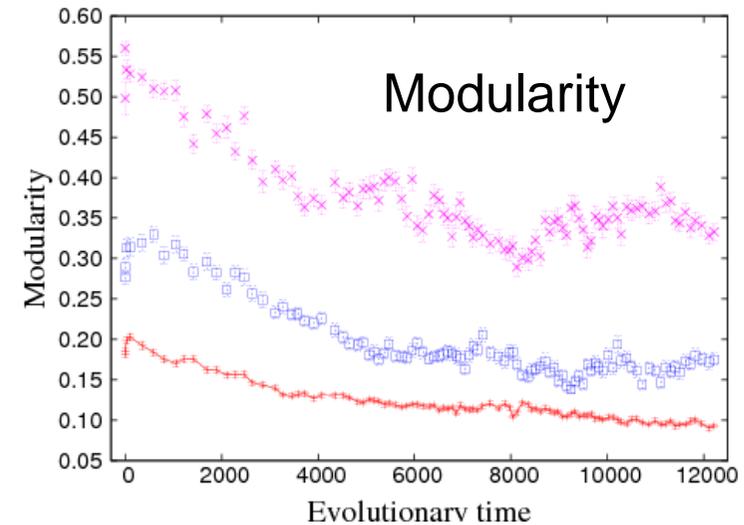
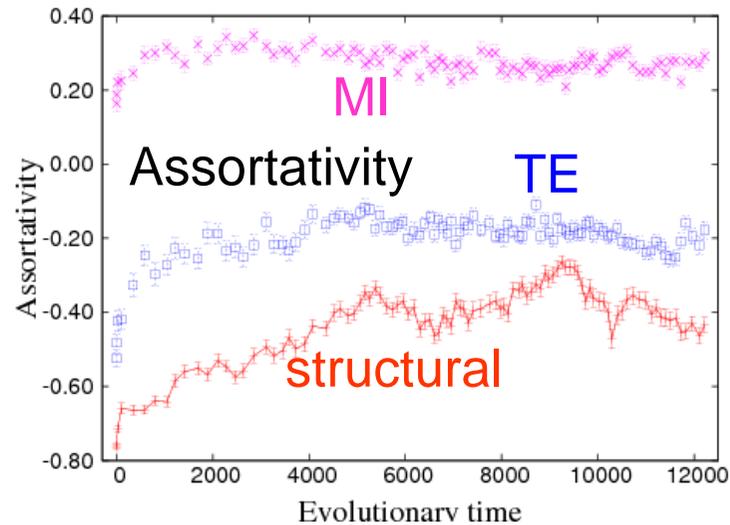
- Clustering Coefficient of a node characterizes the density of links in the environment closest to a vertex
- Formally, the clustering coefficient C of a node is the ratio between the total number y of links connecting its neighbours and the total number of all possible links between all these z nearest neighbours

$$C = 2y / (z(z - 1))$$

- The clustering coefficient C_{net} for a network is the average C over all nodes

➤ All calculated using the Brain Connectivity Toolbox.

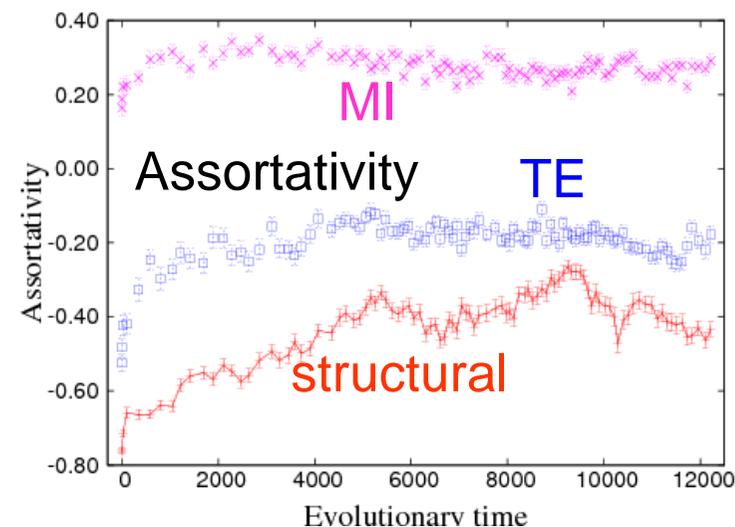
Results (1/4)



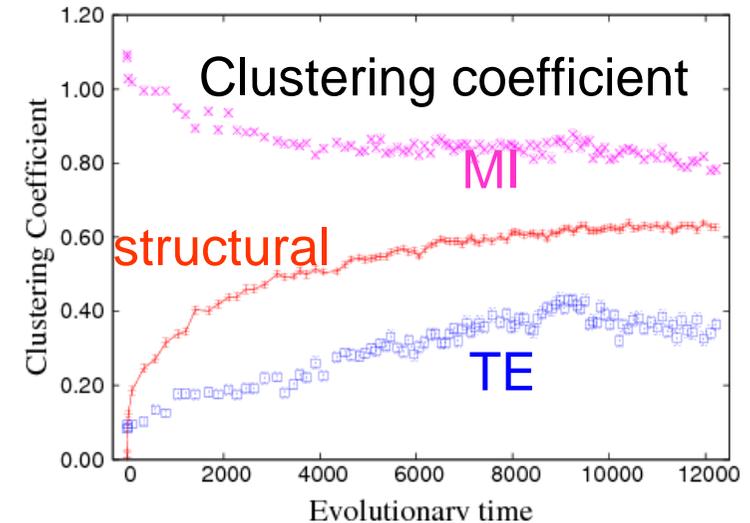
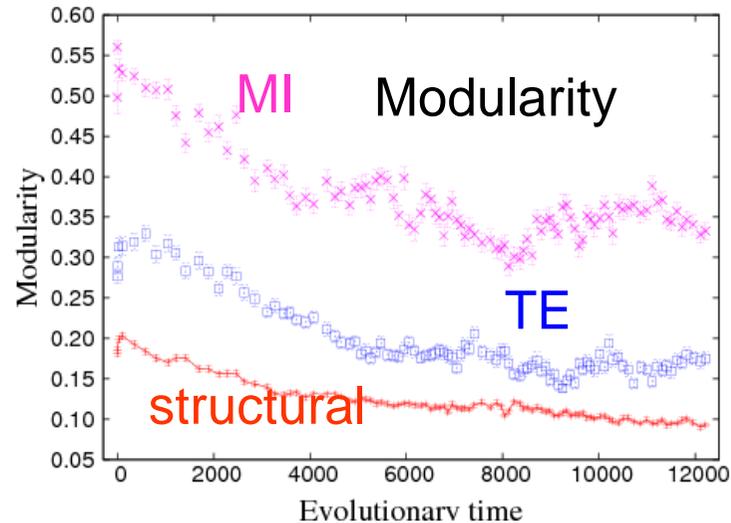
- Topological measures for structural, TE- and MI-inferred networks versus evolutionary time.

Results (2/4)

- **General trends:**
 - All measures reach a steady state once agents have found a good enough solution
 - Transfer entropy trends are more similar to those of the structural network than mutual information
- **Assortativity:**
 - Structural and TE networks are negatively assortative, while MI networks are assortative (all unsurprising).
 - Structural and TE networks become more neutrally assortative over time: possibly an artefact of increased global coupling or increased clustering.



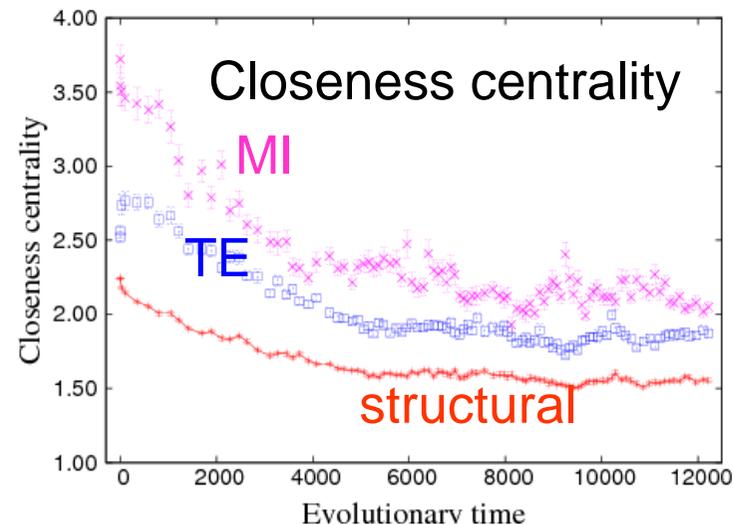
Results (3/4)



- **Modularity and clustering**

- Structural and TE networks become more modular but less clustered: boundaries between modules are blurring, previously separated modules are becoming more strongly clustered both within themselves and across each other.
- MI networks exhibit decreased clustering (relic of the measure)

Results (4/4)



- **Closeness centrality**
 - Reduced for all networks with evo time: expected, as all other results have implied diversification of connectivity across network.
- **Overall**
 - Higher clustering + lower shortest path length → more small-world like with evo time

Conclusion

- Clear trends in structural and functional networks in ANNs of agents in Polyworld in evolutionary time
 - Higher clustering
 - Lower shortest path lengths
- } More small-world character
- Transfer-entropy inferred networks reflect trends in structural networks better than mutual information-inferred networks.
 - Future work
 - Evaluate statistical significance of trends (multiple runs), and contrast with genetic drift.

Information dynamics of cascading failures in power grids

- Small failures in power grids can lead to large cascading failures that cause large and sustained power blackouts.
- There is an obvious need to understand and avoid these events
- Q: How is information intrinsically processed during these events?
 - Key question because network is technically *computing* it's new stable state (attractor) during these events.
 - Understanding the computation can help understand the dynamics
- We look at information storage and transfer as a function of network capacity.
 - Also examine relationship between local topological structure and information dynamics,
 - And relationships in time between information transfer and cascade spreading.

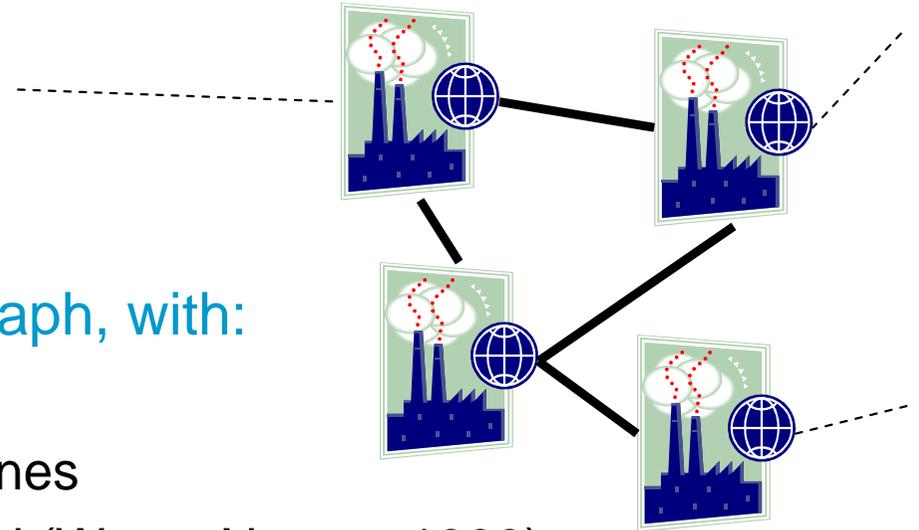
Cascading failure events

- Energy, comms, transport, financial networks are all subject to cascading failure events:
 - local failures that trigger avalanche mechanisms with large effects over the whole network.
- Our focus is energy networks:
 - Usage has increased faster than investment
 - More frequent outages
- Cascading failures are akin to studies of damage spreading / perturbation avalanches
 - Unanswered questions over the relationship of these events to the concept of information transfer.
 - Is information transfer related to the size of avalanche (e.g. Langton, 1990) or the uncertainty in the size of the avalanche (e.g. Ramo et al, 2007) ?
 - How is information transfer affected by network structure?

Cascading failures model

From Crucitti et al, PRE, 2004:

- Network is weighted undirected graph, with:
 - Nodes representing substations
 - Edges representing transmission lines
 - Topology of US Western power grid (Watts, Nature, 1998)
- Each edge ij has an efficiency $e_{ij}(n) \in (0,1]$, with $e_{ij}(0) = 1$
 - $e_{ij}(n)$ = inverse edge weight
 - Efficiency $\varepsilon_{ij}(n)$ of most efficient path from i to j is inverse of shortest path length.
- Each node i has a load $L_i(n)$ = betweenness centrality of node i at time n .
- Each node has a capacity $C_i = \alpha L_i(0)$, with $\alpha \geq 1$ the network tolerance.



Cascading failures model – dynamics

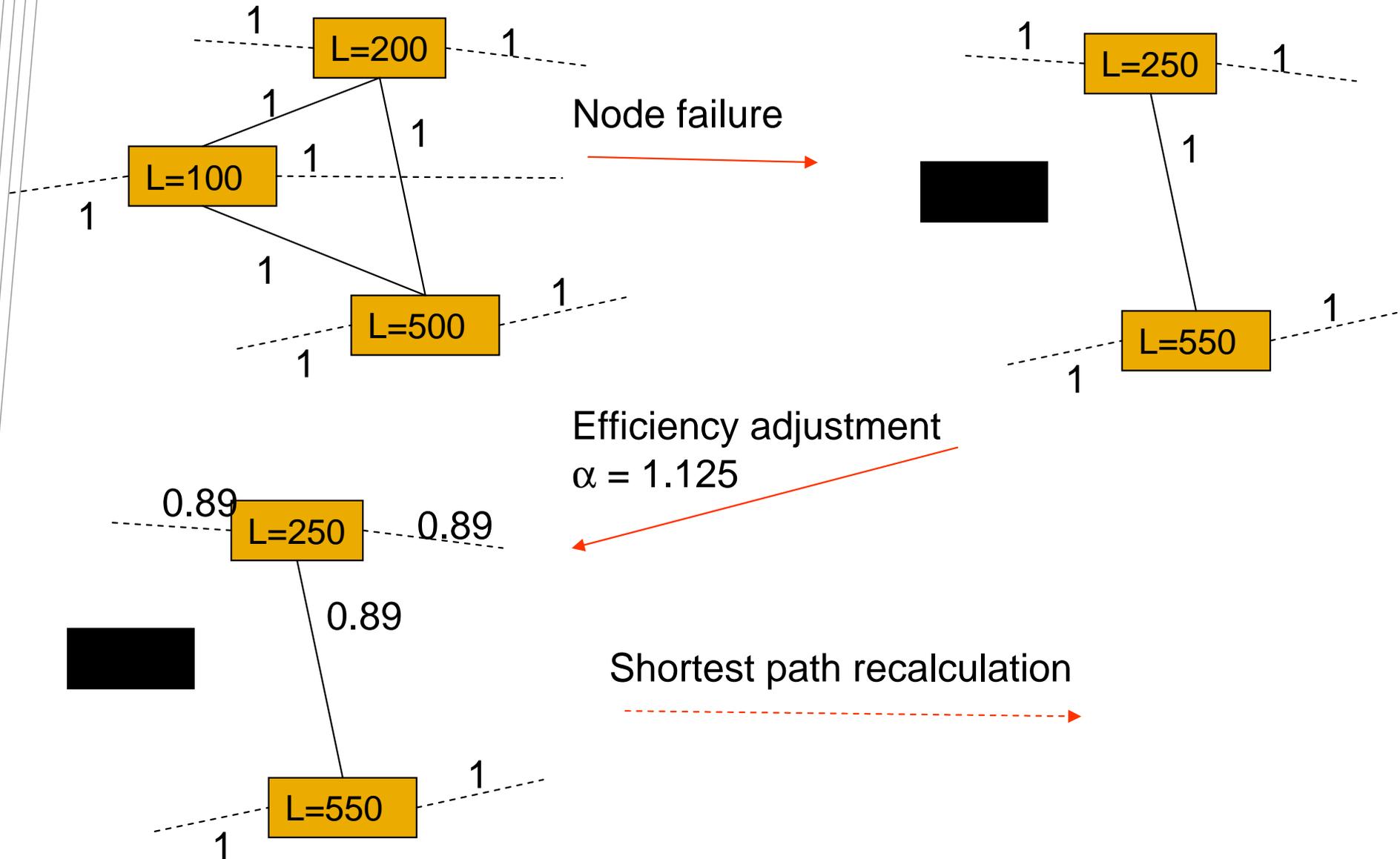
- Edge efficiencies become sub-optimal if (altering original model) either end-point is operating above capacity:

$$e_{ij}(n + 1) = \begin{cases} e_{ij}(0) \min \left(\frac{C_i}{L_i(n)}, \frac{C_j}{L_j(n)} \right) & \text{if } L_i(n) > C_i \text{ or } L_j(n) > C_j, \\ e_{ij}(0) & \text{otherwise .} \end{cases}$$

- Changes in edge efficiencies → changes in most efficient paths → changes in load distribution → changes in edge efficiencies ...
- Initial network state is stable, but removal of a node (simulating initial substation failure) triggers a dynamical process where loads are redistributed.
 - Could cause other nodes to overload, etc, leading to a cascading failure.
 - Stable state may be oscillatory.
- Performance is tracked using average pairwise efficiency:

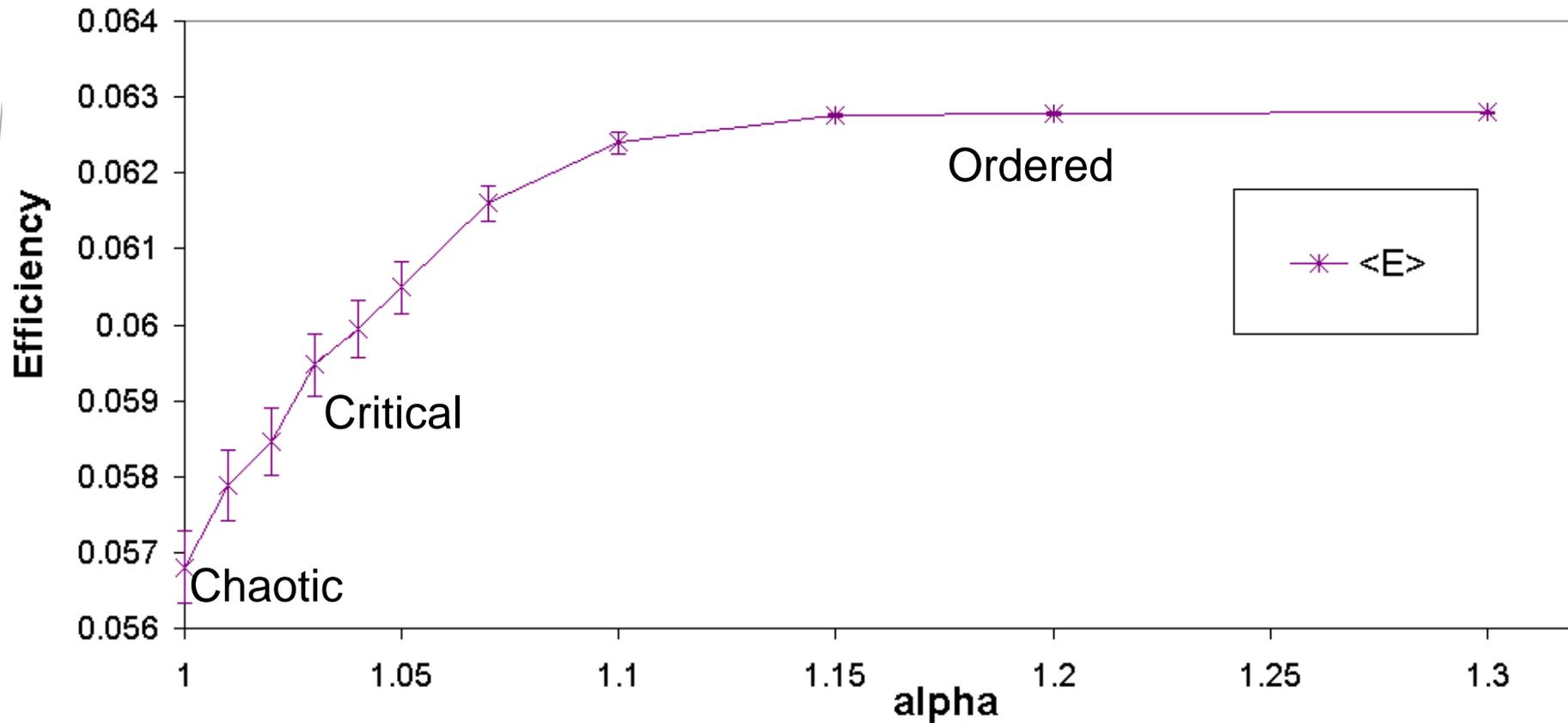
$$E(n) = \langle \epsilon_{ij}(n) \rangle$$

Cascading failures model – example



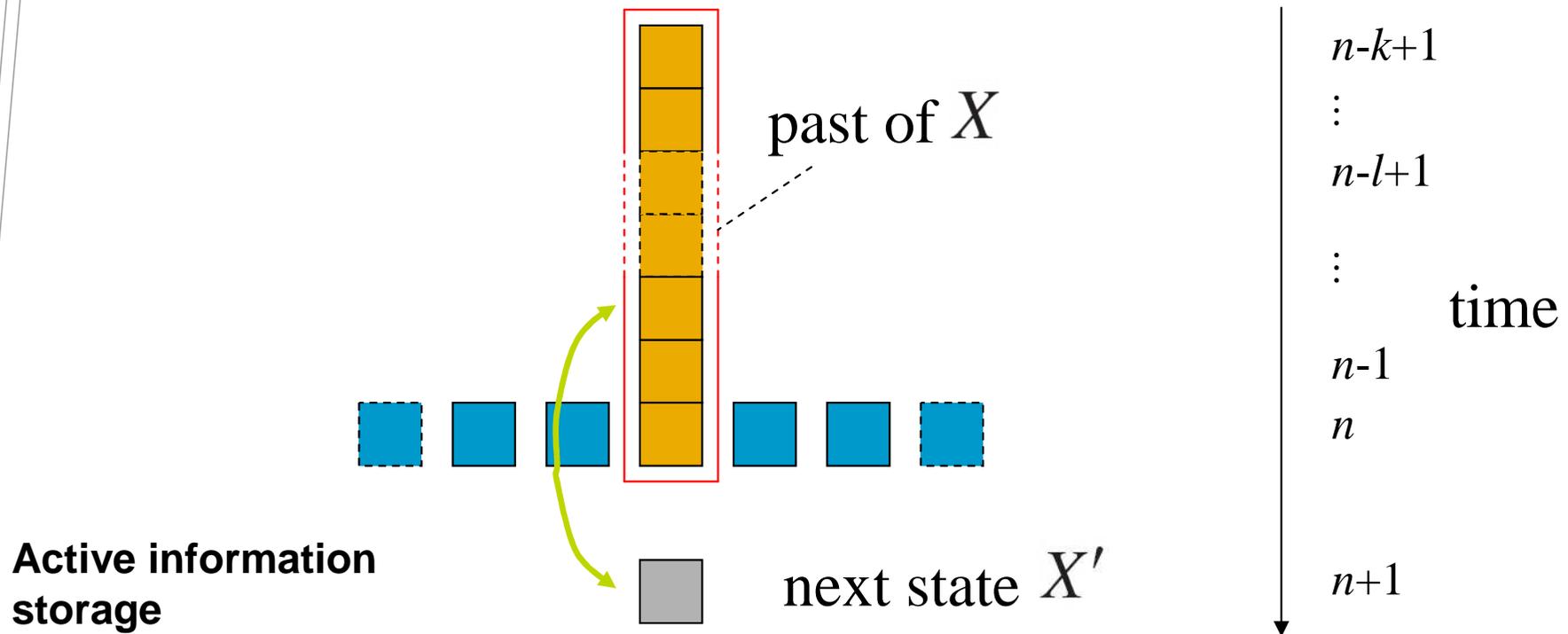
Phase transition with excess capacity alpha

Average information dynamics per causal link versus alpha



Active information storage

$$A_X = I(X^{(k)}; X) = \langle i(x_n^{(k)}; x_{n+1}) \rangle$$

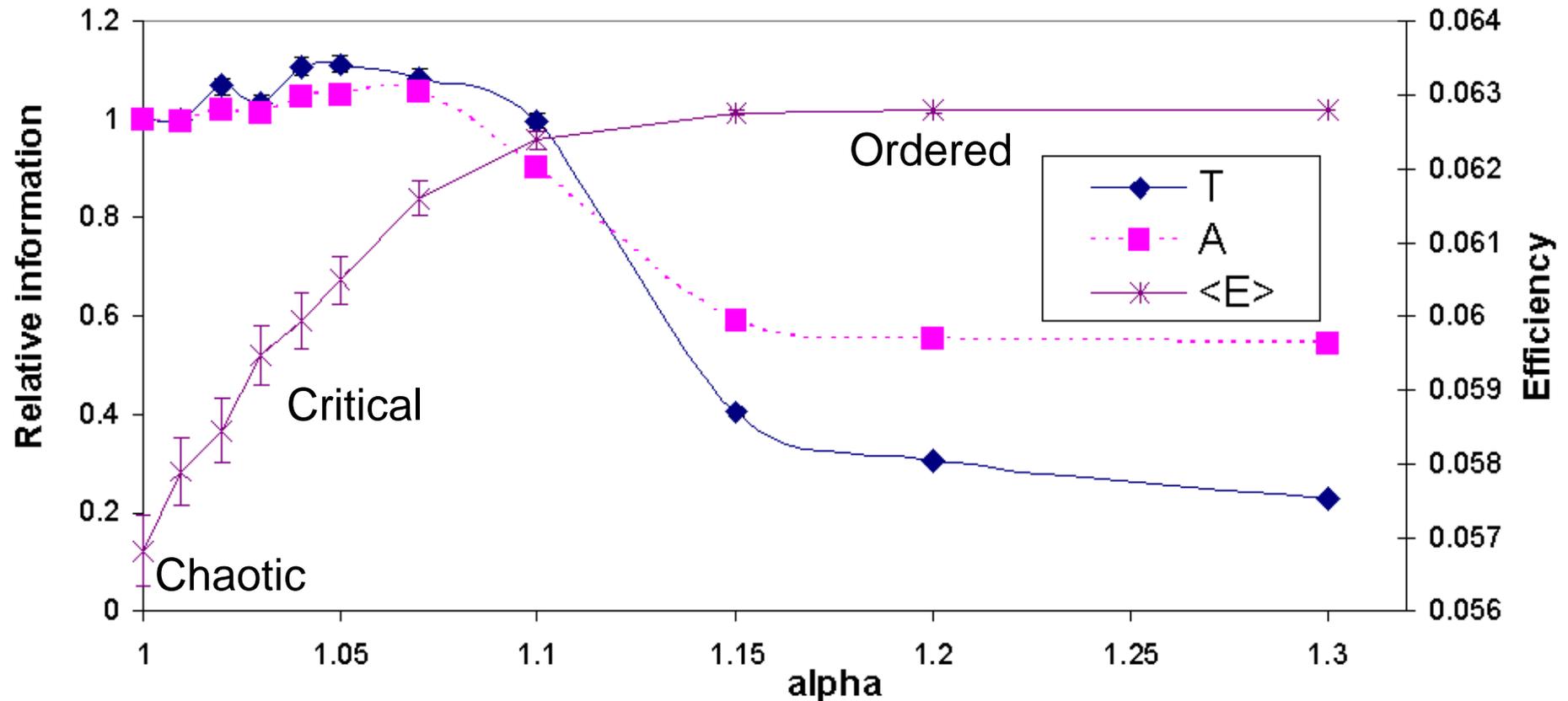


Active information storage

Lizier et al, 2007.

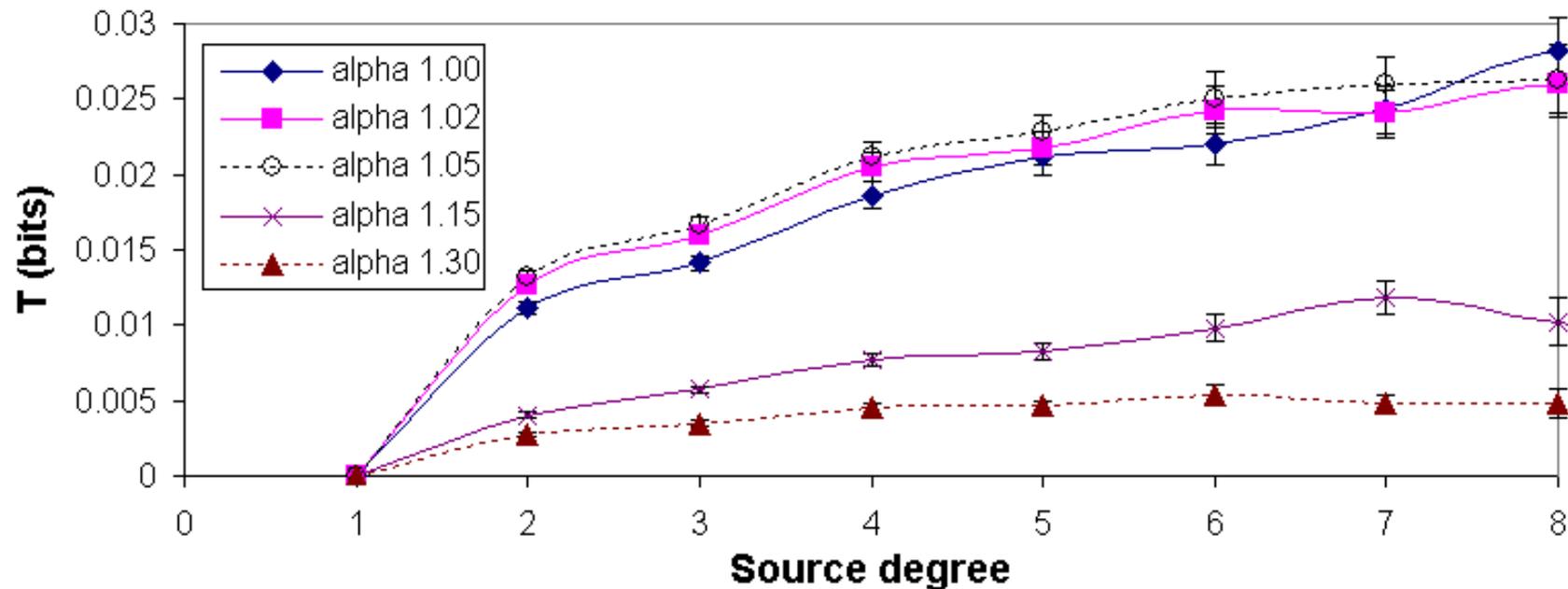
Active info storage = stored information that is currently in use

Results: 1. Info dynamics through phase transition



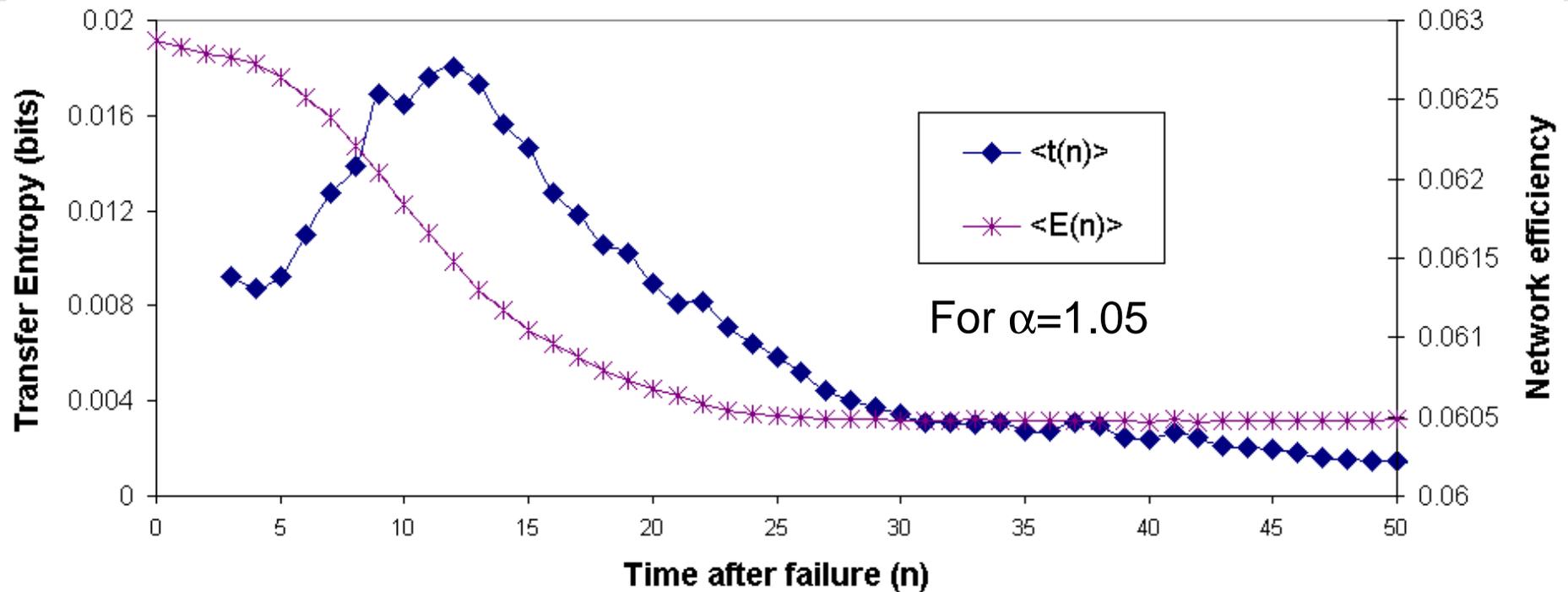
- Both info storage and transfer are maximised near the phase transition in efficiency.
- They change sharply well before efficiency – could be useful early indicators

Results: 2. Info transfer correlated with source degree



- In vicinity of phase transition, info transfer is correlated with degree of source node.
 - More neighbours = more diversity => more info to transfer
- Also a small correlation between info transfer and initial load (b/w centrality) of source node.

Results: 3. Info transfer evolution in time



- Peak in transfer lags the failure event, but coincides with steepest drop in efficiency.
- Large correlation b/w transfer and change in efficiency.
- No correlation to local loads – this seems to be an emergent effect.

Conclusion

- Characterised information dynamics of the intrinsic computation during cascading failures:
 - Maximising of computational capabilities near the phase transition.
 - Local info dynamics correlated with (source) degree.
 - Strong relationship between spread and application independent information transfer.
- Future work
 - Alter model to more realistically reflect power loads
 - Effect of altering topology of power grid, especially including mini-grids
 - Can our knowledge be used to control cascade events?

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Thank you

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